

# Active Modal Control Applying in a 2DOF Structure

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*Abstract: This paper proposes an active modal control technique through electromagnetic actuators, which is applied to a structure with two degrees of freedom. To develop an effective control, it is necessary to build mathematical models capable of accurately representing the dynamic behavior of the mechanical system. The experimental characterization of the mechanical system of two degrees of freedom consists in identifying the unknown parameters through the solution of an inverse problem by using the optimization technique namely differential evolution. From the estimated parameters, it is possible to apply the active modal control to the system. The modal control was used since it allows the control of the vibration amplitude corresponding to a specific mode shape. The control was based on two different approaches. The first one is based on the neuro-fuzzy modal control and the second is based on the fuzzy logic approach. In the experimental tests, a state observer was included to estimate the modal states of the system. Numerical and experimental results demonstrate the effectiveness of the adopted control strategies considering the reduction of the vibration amplitudes.*

**Keywords:** active modal control, neuro-fuzzy modal, fuzzy modal.

## INTRODUCTION

Undesired oscillations may occur in structures when subjected to dynamic forces. Different control methods are used to minimize these oscillations. Active vibration control applies secondary forces in the structure by using various types of actuators (Zang et al., 2016). Among the active control methods, the modal control technique demonstrated to be an interesting approach in previous applications. The modal control is based on a transformation from physical to modal space. Modal controllers can be designed by using various techniques, such as the fuzzy logic. The architecture of control based on fuzzy logic does not require the mathematical model of the system to be controlled. The human experience and expertise to implement the fuzzy controller through linguistic terms are used instead (Gomide and Pedrycz, 2006). However, the accuracy of the fuzzy control is associated with the effective determination of these linguistic terms. The fuzzy controller can be adapted by modifying its parameters and employing learning techniques (Pourzeynali et al., 2007). Systems that have integrated artificial neural networks with fuzzy logic are called neuro-fuzzy systems, which incorporate the advantages of artificial intelligence, such as its capability of learning, with the advantages of fuzzy systems.

In the present contribution, the experimental tests were performed in a mechanical system with two DoFs. The unknown parameters of the system were determined by comparing experimental and simulated frequency response functions (FRFs). In this sense, the optimization algorithm known as differential evolution was used. Finally, the dynamic response of the system containing fuzzy and neuro-fuzzy modal controllers were evaluated both numerically and experimentally.

## Structure Identification

The analyzed structure is represented by a system of two degrees of freedom that is represented by Eq. (1):

$$[m]\{\ddot{d}(t)\} + [c]\{\dot{d}(t)\} + [k]\{d(t)\} = \{f(t)\} \quad (1)$$

where  $[m]$ ,  $[k]$ , and  $[c]$  are the mass, stiffness, and damping matrices, respectively,  $\{f(t)\}$  is the force vector, and  $\{d(t)\}$  is the displacement vector.

The identification of the unknown parameters of the two DoFs structure (i.e., stiffness and damping coefficients) was performed by solving a typical inverse problem, which consists of minimizing the difference between numerical and experimental FRFs by using the above mentioned optimization technique.

The acquisition system showed in Fig. 1 was used to obtain the experimental FRFs. The Data Physics Quattro<sup>®</sup> acquisition board measures the excitation force applied to the system by using an impact hammer and the corresponding

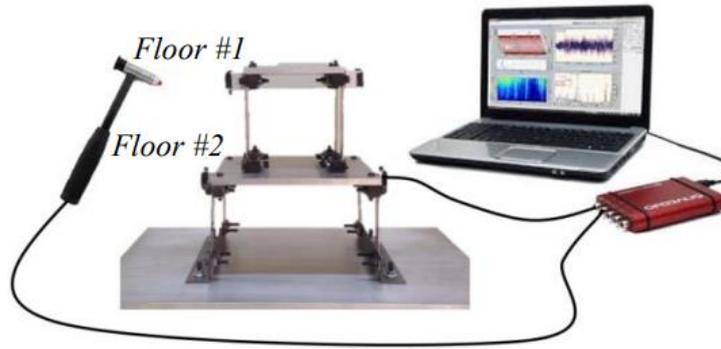


Figure 1 – Identification data acquisition system.

vibration responses are measured by using an accelerometer. The input and output signals were treated through the software SignalCalc ACE<sup>®</sup>. This procedure was performed sequentially involving five tests to obtain average values for the FRFs. In this case, four FRFs were obtained by performing impacts and measuring the vibration responses along the floors #1 and #2 (see Fig. 1).

The differential evolution optimization algorithm (Viana, 2008) was applied by considering a different number of individuals in the initial population: 50, 100, 150, and 200. The unknown parameters and associated design intervals adopted in the optimization problem are shown in Tab. 1. Figure 2 shows the comparison between the experimental FRFs.

Table 1 – Design space adopted in the optimization process.

Parameters	Design Space
Stiffness $k_{floor\#1}$ [N/m]	$9000 \leq k_1 \leq 40000$
Damping $c_{floor\#1}$ [N.s/m]	$0 \leq c_1 \leq 25$
Stiffness $k_{floor\#2}$ [N/m]	$8000 \leq k_2 \leq 20000$
Damping $c_{floor\#2}$ [N.s/m]	$0 \leq c_2 \leq 10$

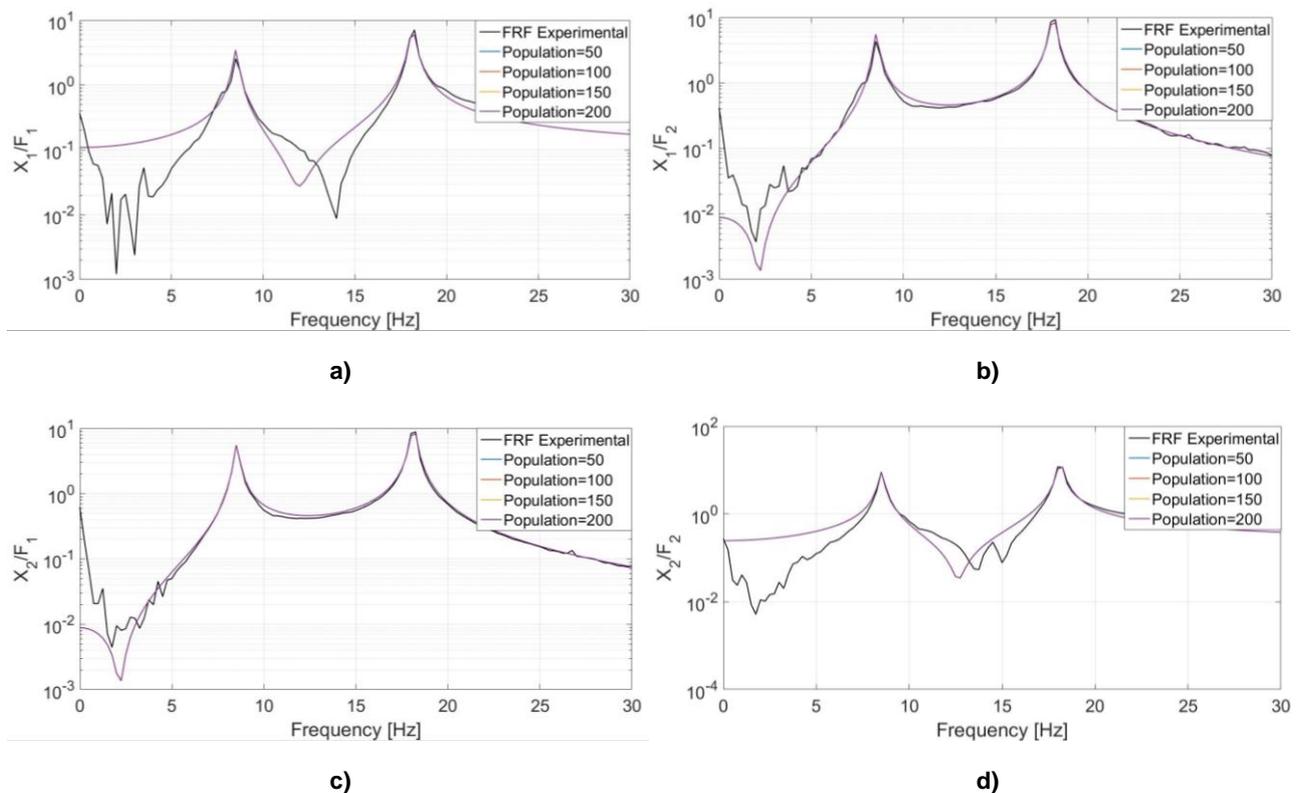


Figure 2 – Experimental and identified FRFs: a) impact at floor #1 and measurement of floor #1; b) impact at floor #1 and measurement of floor #2; c) impact at floor #2 and measurement of floor #1; d) impact in floor #2 and measurement of floor #2.

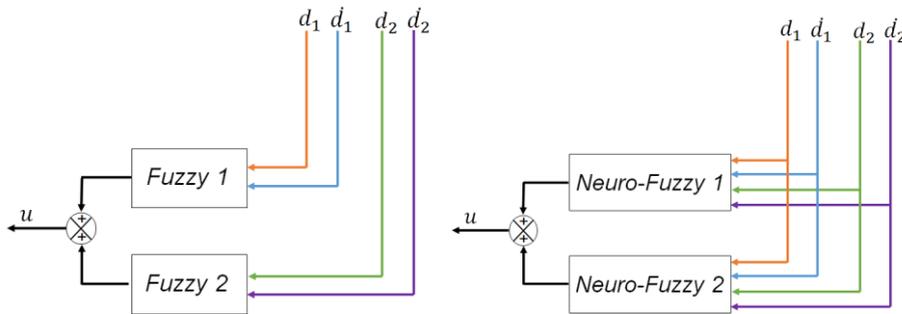
Figure 2 shows the comparison between the experimental and simulated FRFs for the corresponding number of individuals in the initial population of the optimization problem. Note that there is a small variability on the identified FRFs according to the number of individuals used in the initial population of the optimizer. Additionally, the numerical and experimental FRFs are similar, thus demonstrating the representativeness of the identified model. It can be observed that the stiffness and damping parameters used are those obtained for the population of 50 individuals. The parameters of the system are shown in Tab. 2.

**Table 2 – Parameters obtained in the optimization.**

Parameters	Value
Mass $m_1$ [kg]	4.38
Stiffness $k_1$ [N/m]	$2.15 \times 10^4$
Damping $c_1$ [N.s/m]	14.43
Mass $m_2$ [kg]	1.94
Stiffness $k_2$ [N/m]	$3.18 \times 10^{-8}$
Damping $c_2$ [N.s/m]	0.622

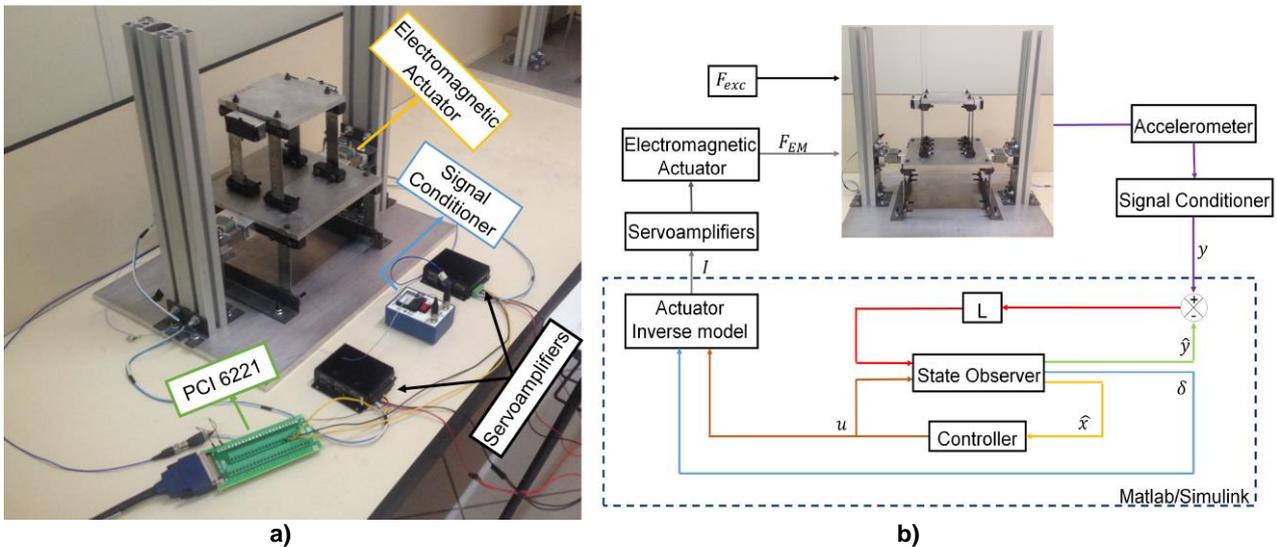
### Control Approach

An active control approach was applied to the two DoFs structure through the fuzzy and neuro-fuzzy modal controllers, in which an electromagnetic actuator provided the control effort. A state observer was used to estimate the modal states of the system. Figure 3 shows the controller scheme. In this case, both *Fuzzy 1* and *Neuro-Fuzzy 1* controllers were designed aiming to attenuate the vibration amplitude of the first vibration mode of the structure. *Fuzzy 2* and *Neuro-Fuzzy 2* controllers are devoted to the second vibration mode of the structure.



**Figure 3 – Modal controllers.**

Figure 4 shows the experimental setup and the control strategy adopted in the present contribution, where  $F_{exc}$  is



**Figure 4 – a) Experimental control and acquisition system; b) control strategy.**

the excitation force applied in the system,  $F_{em}$ , is the actuator control force,  $y$  is the output vector,  $\hat{x}$  is the estimated state vector,  $\hat{y}$  is the estimated output vector, and  $\delta$  is the displacement of the controlled floor (*Floor #1*). In this case, an accelerometer is used to measure the vibration responses of the structure. The National Instruments® acquisition system PCI-6621 and the software Matlab/Simulink® were used to perform the control.

### Pole placement

The pole placement method consists of determining a state feedback gain, so that the poles of the closed-loop system are placed at any desired locations (Ogata, 2013). Considering the feedback control given by Eq. (2):

$$\{\dot{x}(t)\} = [A]\{x(t)\} + [B]\{u(t)\} \quad (2)$$

where  $[A]$  is the dynamic matrix,  $[B]$  is the input matrix,  $\{x(t)\}$  is the state vector, and  $\{u(t)\}$  is the input force. Substituting in Eq. (2) the signal of state feedback control as given by  $\{u(t)\} = -[G]\{x(t)\}$ :

$$\{\dot{x}(t)\} = ([A] - [B][G])\{x(t)\} \quad (3)$$

The gain  $[G]$  can be determined by using the Ackermann's formula. Thus:

$$[G] = [0 \ 0 \ \dots \ 0 \ 1] * [B \ : \ AB \ : \ \dots \ : \ A^{n-1}B]^{-1} * \phi A \quad (4)$$

where  $\phi A$  is given by Eq (5).

$$\phi A = A^n + \alpha_1 A^{n-1} + \dots + \alpha_{n-1} A + \alpha_n I = 0 \quad (5)$$

### Fuzzy Logic

The Fuzzy Inference System is composed of the following components: fuzzification, knowledge base, inference engine, and defuzzification. In the fuzzification, two membership *gbell* functions are used, as given by Eq (6).

$$\mu_i(z) = \frac{1}{1 + \left| \frac{x(t) - P}{L} \right|^{2H}} \quad (6)$$

where  $L$ ,  $H$ , and  $P$  are the parameters of the *gbell* function. Figure 5 shows the degree of membership of the *gbell* function for the input values.

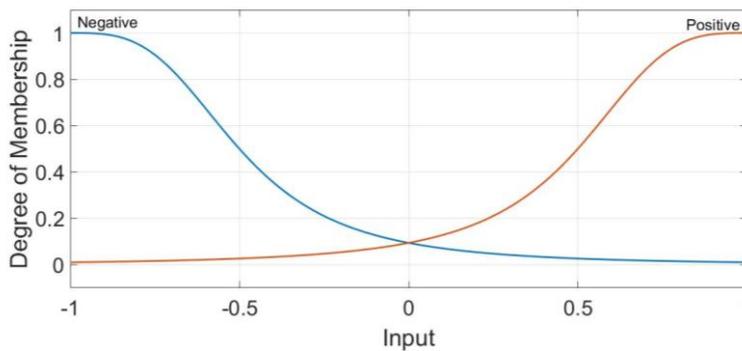


Figure 5 – Fuzzy membership function.

The controller rules are presented in Tab. 3 and Tab. 4, where four rules were created in the conditional statement (If-then) for each controller. The inference engine adopted was Takagi-Sugeno, with output values presented in Eq (7).

$$z_1 = 0, \quad z_2 = [-112.8 \ 40.7 \ 0]\{x\} \quad \text{and} \quad z_3 = [-51.85 \ 40.92 \ 0]\{x\} \quad (7)$$

### Neuro-Fuzzy

The Neuro-Fuzzy structure was chosen as based on the architecture developed by Jang (1993), called Adaptive Neuro-Fuzzy Inference System (ANFIS). The neuro-fuzzy modal control uses the optimized parameters of the

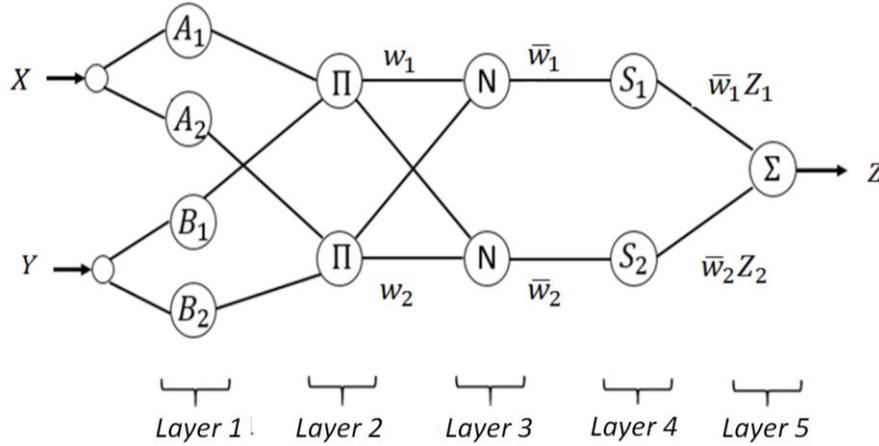
**Table 3– Fuzzy 1 controller rules.**

Rules	$x_1$	$\dot{x}_1$	Output
1	Positive	Positive	$z_2$
2	Positive	Negative	$z_1$
3	Negative	Positive	$z_1$
4	Negative	Negative	$z_2$

**Table 4– Fuzzy 2 controller rules.**

Rules	$x_2$	$\dot{x}_2$	Output
1	Positive	Positive	$z_3$
2	Positive	Negative	$z_1$
3	Negative	Positive	$z_1$
4	Negative	Negative	$z_3$

fuzzy controller by using a neural network approach, in which the objective function is the learning of the desired input-output pairs. For simplicity, the ANFIS architecture considered two inputs,  $X$  and  $Y$ , and an output  $Z$ , as illustrated in Fig. 6.



**Figure 6 – ANFIS architecture.**

In *layer 1*, the membership degree of the inputs  $X$  and  $Y$  is calculated, as given by Eq (8).

$$\mu_{A_i}(X), \mu_{B_i}(Y), i = 1,2, \tag{8}$$

In *layer 2*, each node output represents the degree of applicability of a rule, resulting in Eq (9).

$$w_i = \mu_{A_i}(X) \times \mu_{B_i}(Y), i = 1,2. \tag{9}$$

In *layer 3*, the normalized membership functions are performed. In this layer, the ratio of the  $i$ -th rule's applicability with respect to the sum of all rules' firing strengths is calculated, as given by Eq (10).

$$\bar{w}_i = \frac{w_i}{w_1 + w_2}, i = 1,2. \tag{10}$$

In *layer 4*, the parameters are given by Eq (11). The values of  $p_i, q_i$ , and  $r_i$  correspond to constants to be adjusted in the training process.

$$Z_1 = p_1X + q_1Y + r_1, Z_2 = p_2X + q_2Y + r_2 \tag{11}$$

In *layer 5*, there is the defuzzification of the signals that compute the overall output as the sum of all incoming signals, as given by Eq (12).

$$\sum_i \bar{w}_i Z_i = \frac{\sum_i w_i Z_i}{\sum_i w_i}, i = 1, 2. \tag{12}$$

The parameters of each layer are updated according to the training data and the learning process. The hybrid-learning algorithm combines the recursive least-squares estimation method and the backpropagation gradient descent technique.

The Neuro-Fuzzy control was modeled by using the Toolbox ANFIS of Matlab/Simulink®. The same parameters presented for the Fuzzy controller were optimized for the Neuro-Fuzzy controller. The architecture of the neural network used in the present work is depicted in Fig. 7.

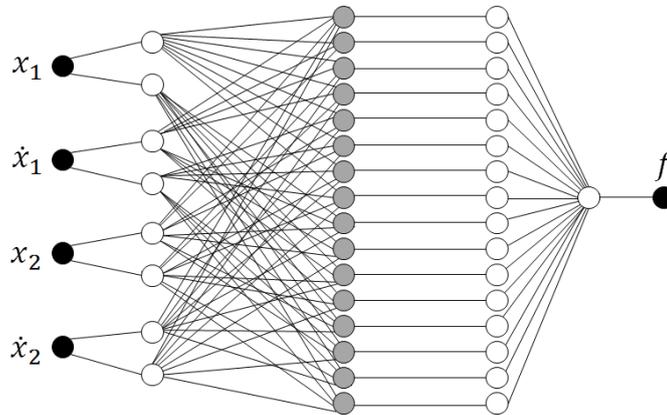


Figure 7 – Neural Network.

The network of neurons has the function of learning based on the desired input-output set. Then, pole placement was performed as the training base for the Neuro-Fuzzy control. The gain of the controller (pole placement) was defined by varying the damping coefficients  $\xi_1$  and  $\xi_2$ . Two control gains were used for training the Neuro-Fuzzy controller, being one for the first vibration mode (*Neuro-Fuzzy 1*) of the structure and another for the second vibration mode (*Neuro-Fuzzy 2*).

Figure 8 illustrates the responses of the feedback control as obtained by pole placement. This is performed by varying the damping coefficient  $\xi_1$ . Note that the amplitude of the first natural frequency decreases as  $\xi_1$  increases. However, by increasing the damping coefficient results a spillover condition at the second natural frequency. Figure 8b shows that the vibration amplitude decreases as  $\xi_1$  increases. However, it can be observed that the vibration component associated with the second vibration mode appears in the vibration responses for values of  $\xi_1$  close to its critical value.

Similar analysis was applied for the second vibration mode of the system by varying  $\xi_2$  (see Fig. 9). In this case, spillover is observed for the first natural frequency as  $\xi_2$  increases. The time domain vibration responses according to  $\xi_2$  are illustrated in Fig. 9b.

The damping coefficients  $\xi_1 = 0.05$  and  $\xi_2 = 0.0078$  were used to obtain the training data training data for the Neuro-Fuzzy 1 controller. Note that  $\xi_1 = 0.05$  reduced the vibration amplitude of the first vibration mode without

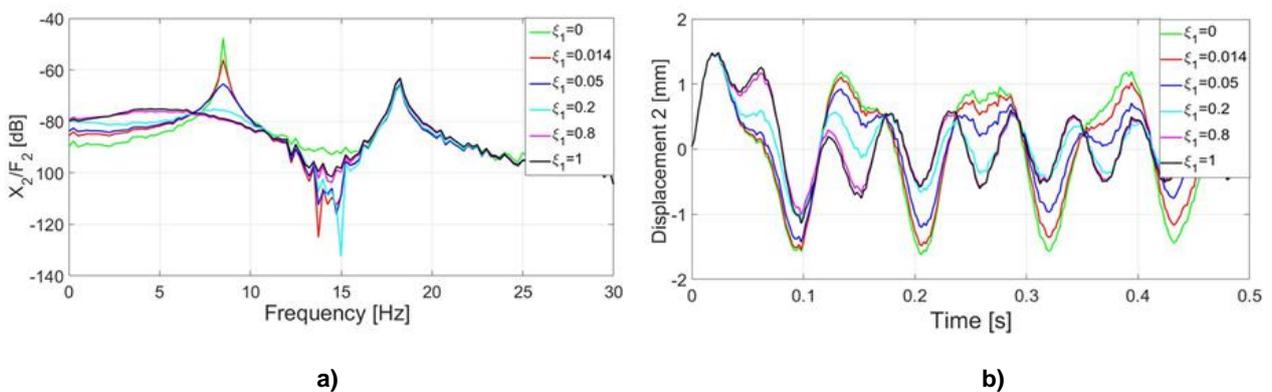


Figure 8 – a) Simulated FRFs; b) simulated impact response.

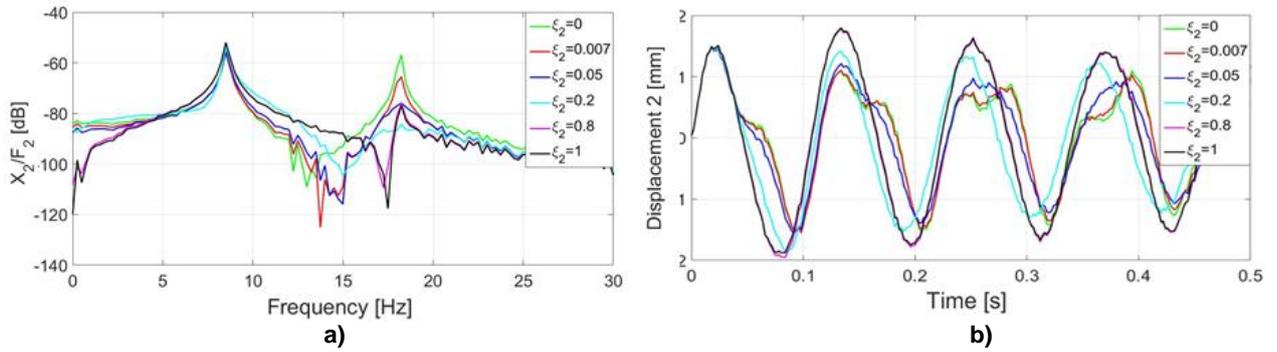


Figure 9 – a) Simulated impact response for different values of  $\xi_2$  ; b) simulated FRFs for  $\xi_2$  .

increasing the spillover in the second mode. The training base of the *Neuro-Fuzzy 2* controller presented the same criteria used for the *Neuro-Fuzzy 1* controller. Therefore, the damping coefficients were  $\xi_1 = 0.015$  and  $\xi_2 = 0.03$ .

For the ANFIS training, the input parameters were the following: error tolerance equal to zero, hybrid training, and 100 training epochs. Figure 10 shows the degree of membership obtained after the training of the *Neuro-Fuzzy1* control and Fig. 11 shows the results associated with the *Neuro-Fuzzy2* controller.

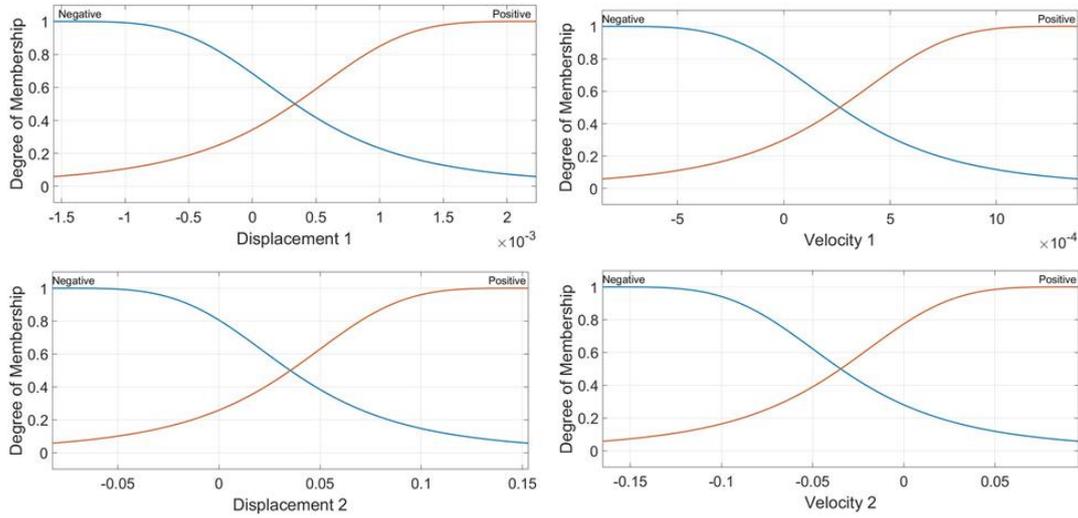


Figure 10 – Membership function *Neuro-Fuzzy1*.

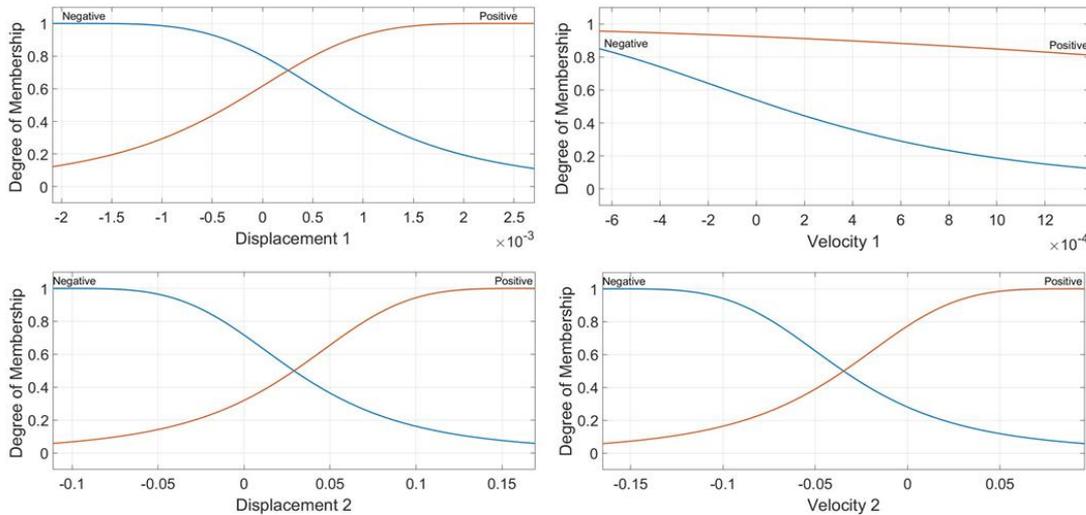


Figure 11 – Membership function *Neuro-Fuzzy2*.

The rules of the controllers are presented in Tab. 5, where sixteen rules have been created in the conditional statement *If-then* for each controller. The inference engine adopted was the Takagi-Sugeno's, with output values presented in Eq (13), where  $\alpha_i, \beta_i, \gamma_i$ , and  $\lambda_i$  are different for each output  $z_i$ .

$$z_i = [\alpha_i \quad \beta_i \quad \gamma_i \quad \lambda_i] \{s\} \tag{13}$$

**Table 5 – Neuro-Fuzzy controller rules.**

Rules	$x_1$	$\dot{x}_1$	$x_2$	$\dot{x}_2$	Output
1	Positive	Positive	Positive	Positive	$z_2$
2	Positive	Positive	Positive	Negative	$z_1$
3	Positive	Positive	Negative	Positive	$z_2$
4	Positive	Positive	Negative	Negative	$z_1$
5	Positive	Negative	Positive	Positive	$z_1$
6	Positive	Negative	Positive	Negative	$z_1$
7	Positive	Negative	Negative	Positive	$z_1$
8	Positive	Negative	Negative	Negative	$z_1$
9	Negative	Positive	Positive	Positive	$z_1$
10	Negative	Positive	Positive	Negative	$z_1$
11	Negative	Positive	Negative	Positive	$z_1$
12	Negative	Positive	Negative	Negative	$z_1$
13	Negative	Negative	Positive	Positive	$z_2$
14	Negative	Negative	Positive	Negative	$z_1$
15	Negative	Negative	Negative	Positive	$z_1$
16	Negative	Negative	Negative	Negative	$z_2$

*Electromagnetic Actuator*

In this work, electromagnetic actuators are used to apply the control forces for active vibration control purposes. The parameters of the actuators are shown in Tab. 6. An inverse model of the electromagnetic actuators is used to determine the electric current required to obtain the control forces, as given by Eq. (14).

**Table 6 – Parameters of the actuators.**

Parameters	Value
$\mu_o$ [H/m]	$4\pi \times 10^{-7}$
$N$	237
$a$ [mm]	9.5
$b$ [mm]	38
$c$ [mm]	28.5
$d$ [mm]	9.5
$f$ [mm]	21.5
$e$ [mm]	2
$\mu_r$	688.27

$$I = \sqrt{\frac{2F_{em} \left( (e \pm \delta) + \frac{b+c+d-2a}{\mu_r} \right)^2}{N^2 \mu_o a f}} \tag{14}$$

where the parameters  $a, b, c, d$ , and  $f$  define the geometry of the solenoid,  $\mu_r$  and  $\mu_o$  are the magnetic permeability and vacuum permeability, respectively,  $N$  is the number of turns,  $e$  is the gap, and  $\delta$  corresponds to the displacement.

## RESULTS

Figure 12 presents the simulated results obtained for the controlled structure when an impact force is applied at the *Floor #2*. The results demonstrate the effectiveness of both control approaches to attenuate the vibration amplitudes of the structure. The amplitude attenuation was obtained for a time smaller than 1 sec for the Neuro-Fuzzy controller and 1.5 s for the Fuzzy controller. Figure 12b shows a significant reduction in the amplitudes of both peaks of the FRF obtained by applying an impact force at the *Floor #2* and performing the response at *Floor #2*. Note that the amplitude of the two vibration modes were attenuated 6.78 dB by using the fuzzy controller and 9.42 dB by using the neuro-fuzzy controller for the first natural frequency and 5.56 dB by using the fuzzy controller and 8.76 dB by using the neuro-fuzzy controller for the second natural frequency. Despite high attenuation of the response was achieved by using the Neuro-Fuzzy controller, the simulations demonstrated high-energy consumption of the actuators as compared with the Fuzzy controller. The control efforts applied by the actuators are presented in Fig. 13.

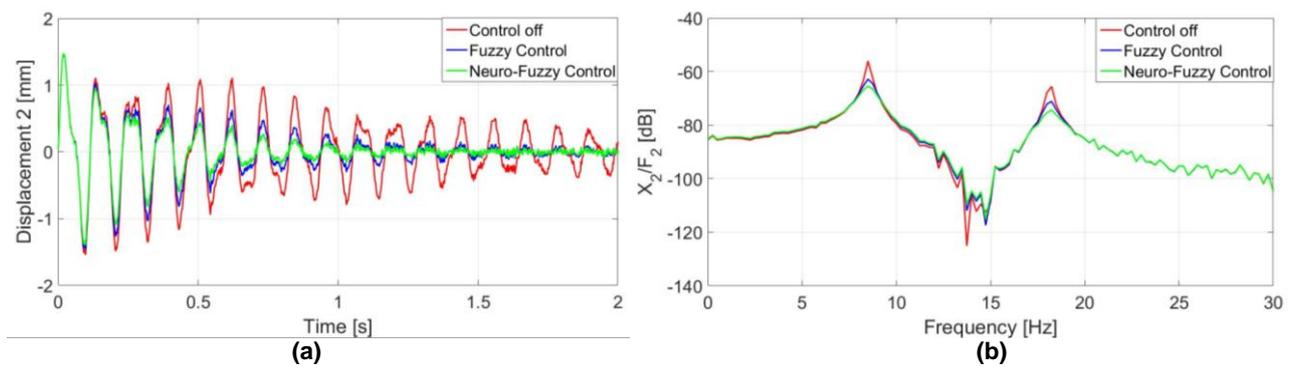


Figure 12 – a) Simulated impact response; b) simulated FRFs.

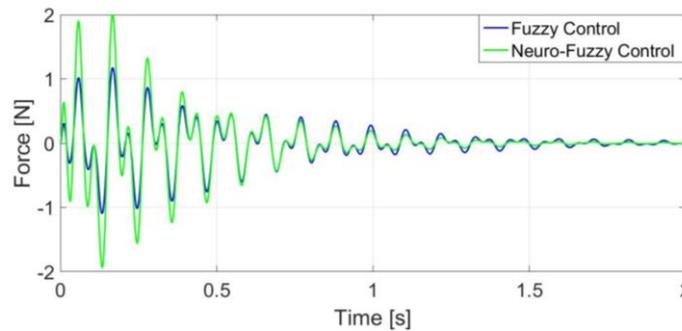


Figure 13 – Simulated control effort.

Figure 14 presents the experimental results. The control effort was applied to the structure by the electromagnetic actuator located at the *Floor #1*. Regarding the impact response (see Fig. 14a), the attenuation time of the oscillations was smaller than 1.5 sec. The FRFs of the system with and without control are depicted in Fig. 14b. Note that both the controllers are able to attenuate the amplitude of the two natural frequencies of the system, namely 7.48dB for the Fuzzy control and 8.90dB for the Neuro-Fuzzy control for the first natural frequency and 7.63dB for the Fuzzy control and 10.14dB for the Neuro-Fuzzy control for the second natural frequency. Figure 15 shows the experimental control effort for the two types of controllers.

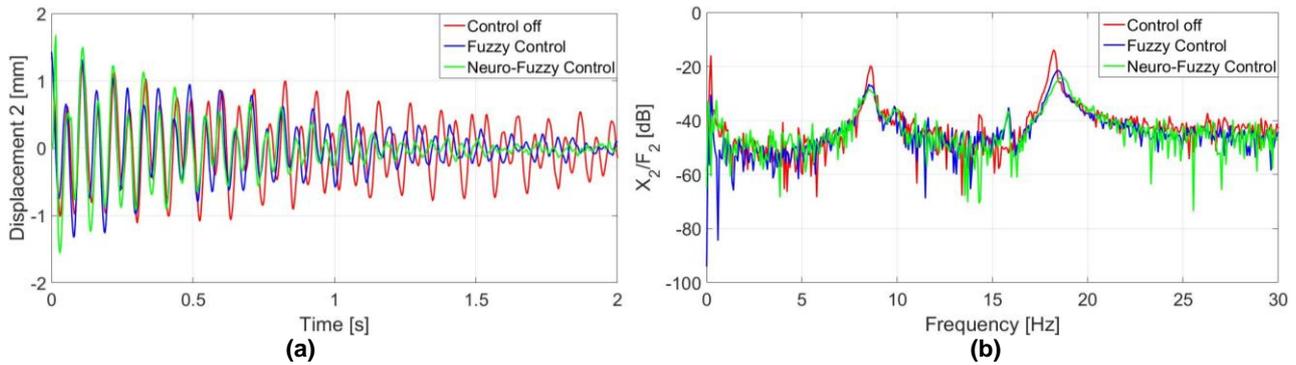


Figure 14 – a) Experimental impact response; b) experimental FRFs.

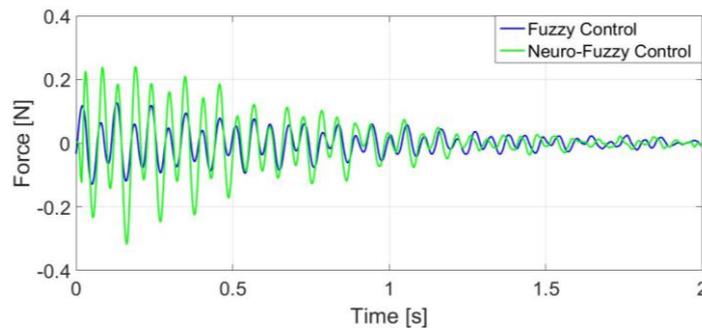


Figure 15 – Experimental control effort.

## CONCLUSION

The obtained results demonstrated the efficiency of the identification methodology to determine the unknown parameters of the 2 DoFs system. The identification of the parameters performed by using the differential evolution technique allowed the characterization of the structure and the model representativeness required by the considered active modal controllers. The numerical and experimental results demonstrated that both designed controllers were efficient to attenuate the vibration responses of the system by using electromagnetic actuators. In general, experimental results are in good agreement with the simulations. The differences between the simulations and experiments since the second natural frequency increases with the control application. The neuro-fuzzy controller showed better results as compared to the fuzzy controller.

## ACKNOWLEDGMENTS

The authors gratefully acknowledge the financial support for this research from CNPq (Process 402581/2016-4), Araucária Foundation and CAPES.

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